## Proving Parallel Lines

## Postulate 1: Converse of Corresponding Angles

In a plane, if two lines are cut by a transversal so that a pair of corresponding angles is congruent, then the lines are parallel


## Theorem 2: Converse of Alternate Interior Angles

In a plane, if two lines are cut by a transversal so that a pair of alternate interior angles is congruent, then the two lines are parallel


$$
\text { If } \angle 1 \cong \angle 2 \text {, then } a \| b \text {. }
$$

## Theorem 2: Converse of Alternate Exterior Angles

In a plane, if two lines are cut by a transversal so that a pair of alternate exterior angles is congruent, then the two lines are parallel


$$
\text { If } \angle 3 \cong \angle 4 \text {, then } a \| b \text {. }
$$

## Theorem 3: Converse of Consecutive Interior angles

In a plane, if two lines are cut by a transversal so that a pair of consecutive interior angles are supplementary, then the two lines are parallel


If $m \angle 5+m \angle 6=180$,

## Mathelpers

## Theorem 4

In a plane, if two lines are perpendicular to the same line, then the two lines are parallel


If $a \perp t$ and $b \perp t$, then $a \| b$.

As a summary, to prove that two lines are perpendicular, you have to prove:

- A pair of alternate interior angles are congruent
- A pair of alternate exterior angles are congruent
- A pair of corresponding angles are congruent
- A pair of consecutive interior angles are supplementary
- Two lines are perpendicular to a third line


## Example 1:

Given: transversal t cuts I and n ;
$t \perp I ;|| | n$


Prove: $\mathrm{t} \perp \mathrm{n}$

| Statements | Reasons |
| :--- | :--- |
| 1. $\mathrm{t} \perp \mathrm{I}$ | 1.Given |
| 2. $\mathrm{m} \angle 1=90$ | 2. Def of $\perp$ lines |
| 3. IIIn | 3. Given |
| 4. $\angle 1 \cong \angle 2,(m \angle 1=m \angle 2)$ | 4. Corr. $\angle \mathrm{s}$ Post |
| 5. $\mathrm{m} \angle 2=90$ | 5. Sub |
| 6. $\therefore \mathrm{t} \perp \mathrm{n}$ | 6. Def of $\perp$ lines |

## Example 2:

Given: I II n, m II n
$p$ is a transversal of $I, m$ and $n$.

Prove: III m


Statements
Reasons

| 1. IIIn | 1. Given |
| :--- | :--- |
| 2. $\angle 1 \cong \angle 3$ | 2. Corr $\angle \mathrm{s}$ Post |
| 3. m IIn | 3. Given |
| 4. $\angle 3 \cong \angle \mathbf{2}$ | 4. Corr $\angle \mathrm{s}$ Post |
| 5. $\angle 1 \cong \angle \mathbf{2}$ | 5. Trans prop |
| 6. $\therefore \mathrm{IIIm}$ | 6. Conv Corr $\angle \mathrm{s}$ Post |

## Example 3:

Given: I II $\mathrm{n}, \mathrm{m} \angle 1=m \angle 3$


Prove: p II q

## Statements

| 1. $\mathrm{I} I \mathrm{n}$ | 1. Given |
| :--- | :--- |
| 2. $\mathrm{m} \angle 1=\mathrm{m} \angle \mathbf{2}$ | 2. Corr $\angle \mathrm{s}$ Post |
| 3. $\mathrm{m} \angle 1=\mathrm{m} \angle 3$ | 3. Given |
| 4. $\mathrm{m} \angle \mathbf{2}=\mathrm{m} \angle 3$ | 4. Substitution |
| 5. $\therefore \mathrm{p} \boldsymbol{I I q}$ | 5. Converse of Alt Int $\angle \mathrm{s}$ thm |

