## Percents

## Part A: Percents and Fractions

The word percent means "per hundred". A percent is a ratio whose denominator is 100 . The symbol for percent is \%.

## Writing Percents

Words: In the area model shown, 85 of the 100 squares are shaded. You can say that 85 percent of the squares are shaded.

Numbers: $\frac{85}{100}=85 \% \quad$ Algebra: $\frac{p}{100}=p \%$


Example 1: Write $\mathbf{2 9 \%}$ and $45 \%$ as fractions in simplest form.
a. $29 \%=\frac{29}{100}$
b. $45 \%=\frac{45}{100}=\frac{9}{20}$

Here are some common percent-fraction equivalents that may be useful to memorize.

| Common Percents |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| $10 \%=\frac{1}{10}$ | $20 \%=\frac{1}{5}$ | $25 \%=\frac{1}{4}$ | $30 \%=\frac{3}{10}$ | $40 \%=\frac{2}{5}$ | $50 \%=\frac{1}{2}$ |  |
| $60 \%=\frac{3}{5}$ | $70 \%=\frac{7}{10}$ | $75 \%=\frac{3}{4}$ | $80 \%=\frac{4}{5}$ | $90 \%=\frac{9}{10}$ | $100 \%=1$ |  |

## Part B: Percents and Proportions

A percent bar model compares a part to a base. In the model shown, 35 is the base, and 14 is a part of the base.


The percent bar model shows that 14 is $40 \%$ of 35 or, equivalently, that $\frac{14}{35}=\frac{40}{100}$.

Solving Percent Problems
You can represent " $a$ is $p$ percent of $b$ " using the proportion

$$
\frac{a}{b}=\frac{p}{100}
$$

Where $a$ is a part of the base $b$ and $p \%$, or $\frac{p}{100}$, is the percent.

## Part C: Percents and Decimals

Because $0.25=\frac{25}{100}$ and $\frac{25}{100}=25 \%$, you can say that $0.25=25 \%$.
This relationship suggests the following rules for writing decimals as percents and percents as decimals.

## Percents and Decimals

- To write a decimal as a percent, move the decimal point two places to the right and write a percent sign.
- To write a percent as a decimal, move the decimal point two places to the left and remove the percent sign.

Fractions, Decimals, and Percents: A fraction, a decimal, and a percent can all represent the same number. You can write a fraction as a percent by first writing the fraction as a decimal.

## Part D: The Percent Equation

On June 14, 2002, the distance between Earth and the moon was about 375,000 kilometers. On that day, a traveling asteroid missed Earth by about $32 \%$ of that distance. How far away from Earth was the asteroid at that time?
You have used the proportion $\frac{a}{b}=\frac{p}{100}$ to solve percent problems. When you solve this proportion for $a$ and write $\frac{p}{100}$ as $p \%$, you get the equation $a=p \% \bullet b$.


The Percent Equation
You can represent " $a$ is $p$ percent of $b$ " using the equation

$$
a=p \% \bullet b
$$

where $a$ is a part of the base $b$ and $p \%$ is the percent.

