

Name: _____

Product – to – Sum Formulas

Exercise 1: Use the product – to – sum formulas to write the product as a sum or difference

1) $6 \sin \frac{\pi}{4} \cos \frac{\pi}{4}$

2) $10 \sin 75^\circ \cos 15^\circ$

3) $\cos 2x \cos 4x$

4) $4 \sin \frac{\pi}{3} \cos \frac{5\pi}{6}$

5) $6 \sin 45^\circ \cos 15^\circ$

6) $\cos 3x \cos 7x$

7) $\cos 4x \sin 5x$

8) $\sin 5x \sin 2x$

9) $3 \sin 2x \sin 3x$

10) $\cos 5x \sin 3x$

11) $3 \sin 2\alpha \sin 3\alpha$

12) $5 \cos(-5\beta) \cos 3\beta$

13) $\cos 2\theta \cos 4\theta$

14) $\sin(x+y) \sin(x-y)$

15) $\sin(x+y) \cos(x-y)$

16) $\cos(\theta - \pi) \sin(\theta + \pi)$

17) $\sin(\theta + \pi) \sin(\theta - \pi)$

Exercise 2: Use product-to-sum identities to find the exact value each expression without using calculators.

1) $\cos 15^\circ \cos 75^\circ$

2) $\sin 195^\circ \cos 75^\circ$

3) $\sin 165^\circ \sin 105^\circ$