

Name: _____

Basic Differentiation Rules

Exercise 1: Use derivative rules to find the derivative of the function:

1) $f(x) = 4x^3 - 2x^2 + 4x + 3$

2) $f(x) = \sqrt{x} - \frac{1}{x^3}$

3) $g(x) = (x^2 - 2x + 3)(x^4 - 4x^2 + 7x)$

4) $h(x) = (x^2 - 3x + 7)^5$

5) $f(x) = \frac{2x-3}{x^2+1}$

6) $g(x) = \sqrt{x^2 - 3x}$

Exercise 2: Differentiate with respect to x

1) $f(x) = 4x^2 - 6x + 5$

2) $f(x) = \frac{2}{x^2} - \frac{1}{2x^3} + 3x$

3) $f(x) = x + \frac{1}{2}x^2$

4) $f(x) = 7x^3 - 3x^2 - 31$

5) $f(x) = 4x - \frac{1}{x} + 5$

6) $f(x) = (x^2 + 3)(x - 4)$

7) $f(x) = \left(2 + \frac{1}{x}\right)^2$

8) $f(x) = \sqrt{x} + \frac{1}{\sqrt{x}}$

9) $f(x) = \frac{(x+1)\sqrt{x}}{x^2}$

10) $f(x) = \frac{(x-1)}{x^2\sqrt{x}}$

11) $f(x) = \frac{2x+3}{x}$

12) $f(x) = \frac{(x-1)^2}{x^2}$

Exercise 3: Find the following

1) $\frac{d}{dt}(3t^2 - 7t - 2)$

2) $\frac{d}{du}[(u+1)(u+2)(u+3)]$

3) $\frac{d}{ds}\left(\frac{(s+1)(3-s^2)}{s}\right)$

4) $\frac{d}{df}\left(\frac{1}{f} - \frac{1}{f^2}\right)$

Exercise 4: Differentiate with respect to t

1) $f(t) = (t+1)(2t^2 - 1)$

2) $f(t) = (3t^3 - 1)(t^3 + 1)$

3) $f(t) = t\sqrt{t} + 5 + \frac{3}{t}$

4) $f(t) = (t+1)^3$

5) $f(t) = \frac{t^2 + t + 1}{t}$

6) $f(t) = \frac{t^2 + 2t + 1}{t+1}$

Exercise 5: Let $f(x) = x^3$ and $f^{-1}(x) = \sqrt[3]{x}$. Show that the value of the derivative of f at $(2, 8)$ is the reciprocal of the value of the derivative of f^{-1} at $(8, 2)$.