

Name: \_\_\_\_\_

## Area of a Region between Two Curves

**Exercise 1:** Find the area between x-axis and the curve

- 1)  $y = -x^2 - 2x, \quad -3 \leq x \leq 2$
- 2)  $y = -x^3 - x^2 + 2x, \quad -2 \leq x \leq 1$
- 3)  $y = -x^3, \quad -1 \leq x \leq 3$
- 4)  $y = \sqrt{x} + 1, \quad [0, 4]$

**Exercise 2:** Find the area bounded by the curves

- 1)  $y = x^2, y = x, \quad x = -1, x = 1$
- 2)  $y = (x-1)^3, y = x-1, \quad [0, 2]$
- 3)  $y = 2x, y = 4x - x^2$
- 4)  $y = x^2 - 30, y = 10 - 3x$

**Exercise 3:** Find the area and sketch the graphs

- a. Under the curve  $y = x^2 + 2$  between the interval  $[-1, 5]$
- b. Find the area under the line  $y = \frac{1}{2}x + 2$ , above the parabola  $y = x^2$ , between the y axis and the line  $x=1$

**Exercise 4:** Find the area of the region bounded by the parabola  $y = x^2$  and the line  $y=x+2$ **Exercise 5:** Determine the area of the region between the graphs of  $y = 2 - x^2$  and  $y = x$

**Exercise 6:** Determine the area of the region bounded by the graphs of  $y = x^2 + 3$ ,  $y = -2x$ ,  $x = 0$ , and  $x = 1$ .

**Exercise 7:** Determine the area of the region between the graphs of  $f(x) = 5x^3 - 2x^2 - 18x$  and  $g(x) = 27x - 2x^2$ .

**Exercise 8:** Find the area bounded by  $y = x^2 - 4$ , the  $x$ -axis and the lines  $x = -1$  and  $x = 2$ .

**Exercise 9:** What is the area bounded by the curve  $y = x^3$ ,  $x = -2$  and  $x = 1$ ?

**Exercise 10:** Find the area of the region bounded by the curve  $y = \sqrt{x-1}$  the  $y$ -axis and the lines  $x = 1$  and  $y = 5$ .

**Exercise 11:** Find the area underneath the curve  $y = x^2 + 2$  from  $x = 1$  to  $x = 2$ .

**Exercise 12:** Find the area between the curves  $y = x^2 + 5x$  and  $y = 3 - x^2$  between  $x = -2$  and  $x = 0$ .

**Exercise 13:** Find the area bounded by  $y = x^3$ ,  $x = 0$  and  $y = 3$ .

**Exercise 14:** Find the area bounded by the curves  $y = x^2 + 5x$  and  $y = 3 - x^2$ .

**Exercise 15:** Find the area bounded by the curves  $y = x^2$ ,  $y = 2 - x$  and  $y = 1$ .