

Name: \_\_\_\_\_

## Using Fundamental Identities

1) Simplify each expression

1)  $(3 - 3\sin x)(3 + 3\sin x)$

2)  $\sec^2 x \tan^2 x + \sec^2 x$

3)  $\frac{9}{\tan x + \sec x}$

4)  $(\sin x + 2\cos x)^2 - (\sin x - 2\cos x)^2$

5)  $\frac{1}{1 + \cos \alpha} - \frac{1}{1 - \cos \alpha}$

6)  $\cos^4 \alpha - 2\cos^2 \alpha + 1$

2) Simplify each of the following:

1)  $\sec \theta - \sec \theta \sin^2 \theta$

2)  $\sin \theta \sec \theta \cot \theta$

3)  $\sin^2 \theta (1 + \cot^2 \theta)$

4)  $\sin^2 \theta \sec^2 \theta - \sec^2 \theta$

5)  $\tan^2 \theta \cos^2 \theta + \cot^2 \theta \sin^2 \theta = 1$

6)  $\tan \theta + \frac{\cos \theta}{1 + \sin \theta}$

- 3) If  $\cos \phi = \frac{1}{2}$  and  $\phi$  terminates in quadrant IV, find  $\sin \phi, \tan \phi,$  and  $\sec \phi$
- 4) Evaluate:  $\sqrt{25 + x^2}$  if  $x = 5 \tan \theta$ , knowing that  $\theta$  is Q3
- 5) Show that  $\sin(A + B) \neq \sin A + \sin B$  by substituting  $30^\circ$  for A and  $60^\circ$  for B in both expressions
- 6) If  $\sin \theta = \frac{\sqrt{2}}{2}$  and  $\tan \theta = 1$ . Find all the trigonometric functions of  $\theta$  and the value of the angle  $\theta$
- 7) If  $\sin A = \frac{3}{4}$  and A is an acute angle, calculate  $\cos A$  and  $\tan A$ .
- 8) Given:  $15 \cot A = 8$ , find all the possible values of  $\sin A$  and  $\sec A$ .
- 9) Given  $\sec \theta = \frac{13}{12}$ , calculate all other trigonometric ratios knowing that  $\theta$  is in *QIV*
- 10) If  $\cot \theta = \frac{7}{8}$ , and  $\theta$  is in *QIII*, evaluate:

1) 
$$\frac{(1 + \sin \theta)(1 - \sin \theta)}{(1 + \cos \theta)(1 - \cos \theta)}$$

2)  $\cot^2 \theta$

- 11) Express the ratios  $\cos A, \tan A$  and  $\sec A$  in terms of  $\sin A$ .
- 12) If  $\angle A$  and  $\angle B$  are acute angles such that  $\cos A = \cos B$ , then show that  $\angle A = \angle B$ .
- 13) In  $\square OPQ$ , right-angled at P,  $OP = 7$  cm and  $OQ - PQ = 1$  cm. Determine the values of  $\sin Q$  and  $\cos Q$ .



- 14) In a right triangle ABC, right-angled at B, if  $\tan A = 1$ , then verify that  $2 \sin A \cos A = 1$ .

